

9) Stationary States: Given the simple state function  $\phi(x, t) = \psi(x) \cdot e^{i\omega t}$ . Evaluate the probability distribution  $W(x, t) = \phi^* \cdot \phi$ . What is  $dW/dt$ ?

10) Heisenberg uncertainty: A particle of mass  $M$  is “moving forth and back” with momentum  $\pm p$  in a linear box of length  $L$ . The positional smearing of the stationary quantum state is  $\Delta x^2 = L^{-1} \cdot \int_0^L dx (x - L/2)^2$ . The kinetic energy of the quantum state of quantum number  $n$  is  $T = p^2/2M = n^2\pi^2\hbar^2/2ML^2$ . The momentum smearing for  $\pm p$  is  $\Delta p^2 = \text{Ave}[(0 \pm p)^2] = p^2$ . Evaluate the “fuzziness product”  $\Delta x \cdot \Delta p$ .

11) Order of magnitude of atoms: In an atom with nuclear charge  $+Ze$  the electrons are distributed in  $x$ -direction between  $-R, +R$ ,  $\Delta x \sim R \sim$  atomic radius. The nuclear-electron attraction energy is  $V \sim Ze \cdot -e/R$ . Similarly, the momenta in  $x$ -direction are distributed between  $-P$  and  $+P$ ,  $\Delta p \sim P$  and the kinetic energy is  $T = P^2/2m$ . Assume  $\Delta x \cdot \Delta p \sim n \cdot \hbar$ . Search for the smallest energy. Give  $P, R, T, V, E$ . What are the ratios of  $T : V : E$ ?

12) Heavy Atoms: Choose  $n = 1$ . What is the electron's velocity  $v$  for nuclear charge  $Z$ ? It's relativistic effective mass is not 1 but  $1/\sqrt{1 - (v/c)^2}$ . How does  $R$  change due to relativity? How many % for Hg ( $Z = 80$ )?